Short Communication

Fitting Growth with the Von Bertalanffy Growth Function: A Comparison of Two Captive Maral Populations

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ABSTRACT

In this research, we used the von Bertalanffy curve for the development of a simulation model of the growth of captive marals or Caspian Red Deer (Cervuselaphussibiricus). The data used in this study was from 18 male marals of Russian (n=9) and Kazakh (n=9) origin, managed under similar conditions, and measured for body weight during their growth at 9, 18 and 24 months. The curve results provided \( a = 219.2 \) and \( c = 0.163 \) for the “standard” Bertalanffy model, and \( a = 194.5 \) and \( c = 0.166 \) for the Levenberg-Marquardt model. The Akaike Information Criterion was clearly lower in the latter model (17,751) than in the “standard” one (45,652) but there were differences between the obtained and estimated weights. There were no differences in growth between Russian and Kazakh animals, and studied marals did not reach their full growth (i.e. the asymptotic level) by 2 years of age, although theoretically stags are ready to mate at 24–30 months of age. Poor feeding of stags in early life or during the antler-growing period can decrease antler production by 10–20%, so if the lack of asymptotic level indicates a deficiency in antler production, antler production is below the potential level, probably due to poor nutrition.

Keywords: Caspian deer, Cervuselaphussibiricus, damped least-squares, growth curve, Levenberg-Marquardt optimization.

INTRODUCTION

The maral (Cervuselaphussibiricus) is one of the easternmost subspecies of Red deer, native to areas in Kazakhstan, China, Mongolia and Russia. They are large and strong animals: adult deer can be up to 150 cm high and up to 330 kg in weight for males and 150–250 kg for females (Lunitsyn, 2004). Domestication of marals was initiated by Russian settlers in the Valley of Buhtarma River in the 1840s and breeding development in north-western and central Altai began in the 1870s. They are highly valued in livestock farming for the supposed
healing properties of the young individuals’ antlers, the so-called “Siberian deer antlers” which are used to prepare a stimulating medicinal agent, called pantocrine. Measuring the offspring’s growth and development at different ages gives insight into the intensity of growth and development. The study of growth basically means the determination of the size as a function of age. In classical feeding experiments, the growth rate is as follows: 

\[ y = \frac{\ln W_t - \ln W_0}{\alpha t} \times 100 \]

where \( W_0 \) is the weight at time \( t=0 \) and \( W_t \) is the weight at time \( t \). However, there are a wide range of alternative growth curves that vary in their flexibility and the number of parameters that need to be fitted. A less well-known growth model with two parameters is that of von Bertalanffy, in which \( y = a(1 - be^{-cx}) \), where \( a \) is the asymptotic length, and \( c \) is the growth rate parameter (von Bertalanffy, 1951). The model assumes that the animal grows towards some theoretical maximum length or weight, and the closer the variable gets to the maximum, the slower the rate of size change will be (Fabens, 1965).

Within the Red deer, there is a relationship between antler weight and body weight: each 10 kg increase antler weights by 0.12 kg. So the purpose of this study was to study the growth curve of marals using body weightings two populations using the von Bertalanffy curve. This is the first research of this kind for marals to the authors’ knowledge.

**MATERIALS AND METHODS**

The data used in this study was from 18 male marals of Russian (n=9) and Kazakh (n=9) origin. Local marals were from the peasant farm "Bagration" (East Kazakhstan region, Ulan area, village of Privolnoye, 50° 06’ N, 81° 32’ E). This farm has the status of a pedigree factory for breeding Kazakh white cattle and is also a breeding farm for Simmental cattle. Maral and horse breeding are additional branches. The farm is located in a dry-steppe zone; the climate is sharp continental with large daily and annual fluctuations in temperature, spanning a range from -52.5°C in winter to +40°C in summer.

The average temperature in January is -16°C and in July is +20.5°C. The average annual precipitation is between 180 and 230 mm. Average thickness of the snow cover is 30–40 cm but it can vary between 5 and 80 cm in individual winters. The soils are dark chestnut and solonetsic. Russian marals were obtained from the agricultural production cooperative breeding factory "Tenginsky" (Altai Republic, Ongudai area, village of Tenga, 50° 50’ 34” N, 85° 39’ 22” E). This farm has the status of a pedigree factory for breeding the Altai-Sayan breed of marals. The same animals were measured for body weight during their growth at 9, 18 and 24 months. Measurements were always taken by the same researcher (NK).

The “standard” von Bertalanffy model was studied. Aiming to minimize the bias of log transformation (Smith, 1993), equation parameters were estimated by the Levenberg-Marquardt model, thus improving the fitting (Press et al., 1992). This optimization, also known as the damped least-squares, is used to solve non-linear least-squares problems. The method acts more like a gradient-descent method when the parameters are far from their optimal value. The Akaike Information Criterion (AIC) aided in the selection of the model. AIC deals with the trade-off between the goodness of fit of the model and the complexity of the model, offering a relative estimate of the information lost when a given model is used to represent the process that generates the data.

Lower values for the AIC imply a better fit, adjusted for the number of parameters. The Wilcoxon signed-rank test, a non-parametric statistical hypothesis test, was the used to compare matched samples (real and estimated body weight) to assess whether their population mean ranks differed. Finally, an ANCOVA (Analysis of Covariance) was used to compare models between Russian and Kazakh animals. Statistical treatments were done with PAST v. 2.17c (Hammer et al., 2001).
RESULTS

The results provide $a=219.22$ and $c=0.163$ for the “standard” Bertalanffy model, and $a=194.47$ and $c=0.166$ for the Levenberg-Marquardt model. AIC was lower in the Levenberg-Marquardt model (17,751) than in the “standard” one (45,652), which is shown in Figure 1.

The Wilcoxon test showed statistical differences between the obtained and estimated weights ($W=1275, p<<0.0001$) but – as the model is intended more as an analysis of growth (results are easily interpreted as “growth rates”) than a predictive model – it is acceptable. Moreover, ages are not known exactly for each individual, so only three “estimated body weights” were obtained. Although value $a$ for the Levenberg-Marquardt model – which can be interpreted as the mean body weight the animals reach if they were to grow indefinitely (that is, 187.7–204.4 kg) – is well below the average body weight for 24-month-old animals (205.2±9.05 kg), the curve does not reach an asymptotic level. The high range of weight for this age (140.4–219.0 kg, CV=16.36%) could explain why the real body weights are higher than the fitted weights (Figure 2). ANCOVA showed no differences in growth between Russian and Kazakh animals ($F=0.601, p=0.441$; Figure 3).

DISCUSSION

The von Bertalanffy growth curve implies that the growth rate declines linearly with length. Theoretically, stags are ready to mate at 24–30 months of age, but the studied marals appear to not reach their full growth (i.e. the asymptotic level) by 2 years of age. If the lack of an asymptotic level in the curve indicates a deficiency in body weight (possibly due to poor feeding), antler production will be below its potential level (poor feeding of stags in early life or during the antler-growing period can decrease antler production by 10–20%). In conclusion, maral managers should ensure that the animals’ genetic potential for antler size is not compromised by poor nutrition as appears to occur at present.
Maral growth parameters, of course, can differ from breed to breed and also from stock to stock, which is why further studies with more animals from other stocks and including more age groups would be desirable. When collecting samples for an age/body-weight key, it would also be important to include in the sample some very young, and some very old specimens, with exact age known. When improving management conditions, managers must also consider the genetic influence of dams on antler production because they contribute 50% of the genes for antler production.

CONCLUSION

According to the von Bertalanffy growth curve, stags are ready to mate at 24–30 months of age, but the studied marals appear to not reach their full growth by 2 years of age. If the lack
of an asymptotic level in the curve indicates a deficiency in body weight (possibly due to poor feeding), antler production will be below its potential level.

**Ethics Statement**

No traumatic manipulations were involved in this study.

**Sources of Funding**

None to declare.

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**REFERENCE**


